

## Unit 5.4 Operations with Radical Expressions EXAMPLES

**Simplify.**

1)  $\sqrt{5} + \sqrt{5}$

2)  $\sqrt{3} + \sqrt{3}$

3)  $-3\sqrt{6} - 2\sqrt{6}$

4)  $3\sqrt{6} - \sqrt{6}$

5)  $-\sqrt{5} + 4\sqrt{5}$

6)  $-3\sqrt{72} - 3\sqrt{8}$

7)  $3\sqrt{12} + 3\sqrt{27}$

8)  $-3\sqrt{8} + 3\sqrt{128}$

9)  $4\sqrt{28} - 3\sqrt{8} - 2\sqrt{72}$

10)  $-\sqrt{6} + 3\sqrt{54} - 3\sqrt{8} + 3\sqrt{32}$

11)  $\sqrt{42}(\sqrt{12} + \sqrt{14})$

12)  $-2\sqrt{35}(7 - 2\sqrt{15})$

13)  $5\sqrt{30x}(-2\sqrt{14} + 2\sqrt{6x})$

14)  $\sqrt{5}(\sqrt{7} + 4)$

15)  $(3\sqrt{7} - 2)(-6\sqrt{7} + 6)$

16)  $(\sqrt{7} + \sqrt{6})(-7\sqrt{7} + \sqrt{6})$

17)  $(\sqrt{3} + \sqrt{6n})(-5\sqrt{4n} + \sqrt{6})$

18)  $(-2\sqrt{7} - 6\sqrt{2})(\sqrt{2} + 2\sqrt{2b})$

**Find the conjugate of the denominator.**

$$19) \frac{5}{2 - \sqrt{2}}$$

$$20) \frac{\sqrt{2}}{\sqrt{3} - \sqrt{5}}$$

$$21) \frac{5}{-1 + \sqrt{2}}$$

$$22) \frac{2}{\sqrt{3} + 3}$$

$$23) \frac{\sqrt{2}}{-4 + \sqrt{5}}$$

$$24) \frac{5}{-4 - \sqrt{3}}$$

$$25) \frac{5}{2 - 5\sqrt{2x^2}}$$

$$26) \frac{2}{5 + \sqrt{2n}}$$

$$27) \frac{5x}{\sqrt{3x^4} - 2\sqrt{3x}}$$

$$28) \frac{3}{3 + 5\sqrt{5v^4}}$$

$$29) \frac{5 - \sqrt{2}}{4 - \sqrt{3}}$$

$$30) \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} + \sqrt{2}}$$

$$31) \frac{-1 + 3\sqrt{3}}{\sqrt{5} + 4\sqrt{2}}$$

$$32) \frac{3 - 5\sqrt{5}}{3 + \sqrt{2}}$$

$$33) \frac{2a^2 - 5\sqrt{5a^2}}{3a - \sqrt{a^2}}$$

$$34) \frac{3p - 2\sqrt{3p^2}}{\sqrt{5p^4} + \sqrt{p^3}}$$

## Unit 5.4 Operations with Radical Expressions EXAMPLES

**Simplify.**

1)  $\sqrt{5} + \sqrt{5}$

$2\sqrt{5}$

2)  $\sqrt{3} + \sqrt{3}$

$2\sqrt{3}$

3)  $-3\sqrt{6} - 2\sqrt{6}$

$-5\sqrt{6}$

4)  $3\sqrt{6} - \sqrt{6}$

$2\sqrt{6}$

5)  $-\sqrt{5} + 4\sqrt{5}$

$3\sqrt{5}$

6)  $-3\sqrt{72} - 3\sqrt{8}$

$-24\sqrt{2}$

7)  $3\sqrt{12} + 3\sqrt{27}$

$15\sqrt{3}$

8)  $-3\sqrt{8} + 3\sqrt{128}$

$18\sqrt{2}$

9)  $4\sqrt{28} - 3\sqrt{8} - 2\sqrt{72}$

$8\sqrt{7} - 18\sqrt{2}$

10)  $-\sqrt{6} + 3\sqrt{54} - 3\sqrt{8} + 3\sqrt{32}$

$8\sqrt{6} + 6\sqrt{2}$

11)  $\sqrt{42}(\sqrt{12} + \sqrt{14})$

$6\sqrt{14} + 14\sqrt{3}$

12)  $-2\sqrt{35}(7 - 2\sqrt{15})$

$-14\sqrt{35} + 20\sqrt{21}$

13)  $5\sqrt{30x}(-2\sqrt{14} + 2\sqrt{6x})$

$-20\sqrt{105x} + 60x\sqrt{5}$

14)  $\sqrt{5}(\sqrt{7} + 4)$

$\sqrt{35} + 4\sqrt{5}$

15)  $(3\sqrt{7} - 2)(-6\sqrt{7} + 6)$

$-138 + 30\sqrt{7}$

16)  $(\sqrt{7} + \sqrt{6})(-7\sqrt{7} + \sqrt{6})$

$-43 - 6\sqrt{42}$

17)  $(\sqrt{3} + \sqrt{6n})(-5\sqrt{4n} + \sqrt{6})$

$-10\sqrt{3n} + 3\sqrt{2} - 10n\sqrt{6} + 6\sqrt{n}$

18)  $(-2\sqrt{7} - 6\sqrt{2})(\sqrt{2} + 2\sqrt{2b})$

$-2\sqrt{14} - 4\sqrt{14b} - 12 - 24\sqrt{b}$

**Find the conjugate of the denominator.**

19)  $\frac{5}{2 - \sqrt{2}}$

$$\frac{10 + 5\sqrt{2}}{2}$$

21)  $\frac{5}{-1 + \sqrt{2}}$

$$5 + 5\sqrt{2}$$

23)  $\frac{\sqrt{2}}{-4 + \sqrt{5}}$

$$\frac{-4\sqrt{2} - \sqrt{10}}{11}$$

25)  $\frac{5}{2 - 5\sqrt{2x^2}}$

$$\frac{10 + 25x\sqrt{2}}{4 - 50x^2}$$

27)  $\frac{5x}{\sqrt{3x^4} - 2\sqrt{3x}}$

$$\frac{5x^2\sqrt{3} + 10\sqrt{3x}}{3x^3 - 12}$$

29)  $\frac{5 - \sqrt{2}}{4 - \sqrt{3}}$

$$\frac{20 + 5\sqrt{3} - 4\sqrt{2} - \sqrt{6}}{13}$$

31)  $\frac{-1 + 3\sqrt{3}}{\sqrt{5} + 4\sqrt{2}}$

$$\frac{\sqrt{5} - 4\sqrt{2} - 3\sqrt{15} + 12\sqrt{6}}{27}$$

33)  $\frac{2a^2 - 5\sqrt{5a^2}}{3a - \sqrt{a^2}}$

$$\frac{2a - 5\sqrt{5}}{2}$$

20)  $\frac{\sqrt{2}}{\sqrt{3} - \sqrt{5}}$

$$\frac{-\sqrt{6} - \sqrt{10}}{2}$$

22)  $\frac{2}{\sqrt{3} + 3}$

$$\frac{-\sqrt{3} + 3}{3}$$

24)  $\frac{5}{-4 - \sqrt{3}}$

$$\frac{-20 + 5\sqrt{3}}{13}$$

26)  $\frac{2}{5 + \sqrt{2n}}$

$$\frac{10 - 2\sqrt{2n}}{25 - 2n}$$

28)  $\frac{3}{3 + 5\sqrt{5v^4}}$

$$\frac{9 - 15v^2\sqrt{5}}{9 - 125v^4}$$

30)  $\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} + \sqrt{2}}$

$$\frac{5 - \sqrt{10} + \sqrt{15} - \sqrt{6}}{3}$$

32)  $\frac{3 - 5\sqrt{5}}{3 + \sqrt{2}}$

$$\frac{9 - 3\sqrt{2} - 15\sqrt{5} + 5\sqrt{10}}{7}$$

34)  $\frac{3p - 2\sqrt{3p^2}}{\sqrt{5p^4} + \sqrt{p^3}}$

$$\frac{3p\sqrt{5} - 3\sqrt{p} - 2p\sqrt{15} + 2\sqrt{3p}}{5p^2 - p}$$