

Unit 4.5 Double Angle Identities PRACTICE

Verify each identity.

$$1) \frac{2}{\csc^2 x} = 1 - \cos 2x$$

$$\frac{2}{\csc^2 x}$$

Use $\csc x = \frac{1}{\sin x}$

$$2\sin^2 x$$

Use $\cos 2x = 1 - 2\sin^2 x$

$$1 - \cos 2x$$

■

$$2) \frac{\sin 4x}{\sin 2x} = 2\cos 2x$$

$$\frac{\sin 4x}{\sin 2x}$$

Use $\sin 4x = 2\sin 2x \cos 2x$

$$\frac{2\sin 2x \cos 2x}{\sin 2x}$$

Cancel common factors

$$2\cos 2x$$

■

$$3) \sec^2 x - 2\cos^2 x = -\cos 2x + \tan^2 x$$

$$\sec^2 x - 2\cos^2 x$$

Use $\tan^2 x + 1 = \sec^2 x$

$$\tan^2 x + 1 - 2\cos^2 x$$

Use $\cos 2x = 2\cos^2 x - 1$

$$-\cos 2x + \tan^2 x$$

■

4) $\cos 2x \tan 2x = 2\sin x \cos x$

$$\cos 2x \tan 2x \quad \text{Use } \tan 2x = \frac{\sin 2x}{\cos 2x}$$

$$\frac{\cos 2x \sin 2x}{\cos 2x} \quad \text{Cancel common factors}$$

$$\sin 2x \quad \text{Use } \sin 2x = 2\sin x \cos x$$

$$2\sin x \cos x \quad \blacksquare$$

5) $\frac{\sin 2x}{2\cos^2 x} = \frac{1}{\cot x}$

$$\frac{\sin 2x}{2\cos^2 x} \quad \text{Use } \sin 2x = 2\sin x \cos x$$

$$\frac{2\sin x \cos x}{2\cos^2 x} \quad \text{Cancel common factors}$$

$$\frac{\sin x}{\cos x} \quad \text{Use } \cot x = \frac{\cos x}{\sin x}$$

$$\frac{1}{\cot x} \quad \blacksquare$$

6) $\frac{\sin 2x}{1 + \cos 2x} = \frac{1}{\cot x}$

$$\frac{\sin 2x}{1 + \cos 2x} \quad \text{Use } \sin 2x = 2\sin x \cos x$$

$$\frac{2\sin x \cos x}{1 + \cos 2x} \quad \text{Use } \cos 2x = 2\cos^2 x - 1$$

$$\frac{2\sin x \cos x}{2\cos^2 x} \quad \text{Cancel common factors}$$

$$\frac{\sin x}{\cos x} \quad \text{Use } \cot x = \frac{\cos x}{\sin x}$$

$$\frac{1}{\cot x} \quad \blacksquare$$

7) $\frac{\cot x}{1 + \cos 2x} = \frac{1}{\sin 2x}$

$$\frac{\cot x}{1 + \cos 2x} \quad \text{Use } \cos 2x = 2\cos^2 x - 1$$

$$\frac{\cot x}{2\cos^2 x} \quad \text{Use } \cot x = \frac{\cos x}{\sin x}$$

$$\frac{\cos x}{2\sin x \cos^2 x} \quad \text{Cancel common factors}$$

$$\frac{1}{2\sin x \cos x} \quad \text{Use } \sin 2x = 2\sin x \cos x$$

$$\frac{1}{\sin 2x} \quad \blacksquare$$