

Unit 4.2 Fundamental Identities Advanced PRACTICE

Verify each identity.

$$1) \frac{\csc^2 x}{\sec^3 x} = \frac{\cos x}{\sec^2 x - 1}$$

$$2) \frac{\sin^2 x}{\cos^2 x \cot x} = \tan x \cdot (\sec^2 x - 1)$$

$$3) \frac{\sin x - \tan x}{\tan x} = \tan^2 x + \cos x - \sec^2 x$$

$$4) \frac{\tan^2 x + 1}{\sin^2 x} = \frac{\csc^2 x}{\cos^2 x}$$

$$5) \frac{\cot x}{\sec^2 x + \csc^2 x} = \cos^3 x \sin x$$

$$6) \cot^2 x \csc^2 x \sin^2 x = \csc^2 x - 1$$

$$7) \frac{\cot^2 x}{\csc^2 x + \sec^2 x} = \frac{\cos^3 x}{\sec x}$$

$$8) \frac{\cot^2 x - \csc^2 x}{\cot x} = -\sec x \sin x$$

$$9) -\tan^2 x \csc^2 x = -\tan^2 x - 1$$

$$10) \frac{\cot^2 x \sec^2 x}{\cos^2 x} = \frac{\tan^2 x + 1}{\sin^2 x}$$

$$11) \csc^2 x \cot x \tan x = \cot^2 x + 1$$

$$12) \csc^2 x - 1 = \frac{\cot x \csc x}{\sec x}$$

$$13) \frac{\csc^2 x - 1}{\csc x} = \csc x \cos^2 x$$

$$14) \frac{\cos^2 x}{1 - \csc^2 x} = -\sin^2 x$$

$$15) -\csc x \sin^2 x = \frac{\tan^2 x - \sec^2 x}{\csc x}$$

$$16) \frac{1}{\cos^2 x \csc^2 x} = \sec^2 x - 1$$

$$17) \frac{\csc x}{\csc^2 x - 1} = \sin x \sec^2 x$$

$$18) \cot^2 x + \sec x \cos x = \frac{1}{\sin^2 x}$$