

## Unit 4.1 Fundamental Identities Basic PRACTICE

Verify each identity.

$$1) \cot^2 x + \csc^2 x = \frac{1 + \cos^2 x}{\sin^2 x}$$

$$2) \frac{\tan^2 x}{\sin x \sec^2 x} = \sin x$$

$$3) \frac{1}{1 + \csc x} = \frac{\sin x}{\sin x + 1}$$

$$4) \frac{\cot x}{\cot x + 1} = \frac{\cos x}{\sin x + \cos x}$$

$$5) \frac{\sec x}{\tan x + \sec x} = \frac{1}{1 + \sin x}$$

$$6) \frac{\cos x}{\sec x \cot^2 x} = \sin^2 x$$

$$7) \frac{\cot^2 x}{\sin x} = \frac{\csc x}{\tan^2 x}$$

$$8) \tan x \csc x = \frac{1}{\cos x}$$

$$9) \sec x \cdot (1 + \sec x) = \frac{1 + \cos x}{\cos^2 x}$$

$$10) \frac{\sec^2 x}{\tan^2 x - 1} = \frac{1}{\sin^2 x - \cos^2 x}$$

$$11) \frac{\sin x + \csc x}{\csc x} = 1 + \sin^2 x$$

$$12) \frac{\csc x + 1}{\csc^2 x} = \sin x \cdot (\sin x + 1)$$

$$13) \frac{1 - \csc x}{\csc x} = \sin x - 1$$

$$14) \tan^2 x \cot^3 x = \frac{\cos x}{\sin x}$$

$$15) \frac{\sec^2 x + \cos x}{\sec^2 x} = 1 + \cos^3 x$$

$$16) 1 + \sec x = \frac{1 + \cos x}{\cos x}$$

$$17) \frac{\cot x - 1}{\csc x} = \cos x - \sin x$$

$$18) \frac{\csc x}{1 - \csc x} = \frac{1}{\sin x - 1}$$

$$19) \frac{\sec x + 1}{\sec x} = 1 + \cos x$$

$$20) \frac{\sec x - \tan x}{\sec x} = 1 - \sin x$$

$$21) \frac{\tan^2 x - \sec^2 x}{\csc x} = -\sin x$$

$$22) \sec^2 x - \csc^2 x = \tan^2 x - \cot^2 x$$

$$23) \frac{\sec x + 1}{\sec^2 x} = \cos x \cdot (1 + \cos x)$$

$$24) \frac{1 + \cot^2 x}{\sin x} = \csc^3 x$$