

## Unit 1.3 Using Definitions of the Trigonometric Functions PRACTICE

**Use the appropriate reciprocal identity to find each function value. Rationalize denominators when applicable.**

1)  $\cos \theta$ , if  $\sec \theta = -2.5$

2)  $\cot \theta$ , if  $\tan \theta = -\frac{1}{5}$

3)  $\sin \theta$ , if  $\csc \theta = 3$

4)  $\sec \theta$ , if  $\cos \theta = -\frac{\sqrt{7}}{7}$

5)  $\sin \theta$ , if  $\csc \theta = \sqrt{15}$

6)  $\tan \theta$ , if  $\cot \theta = -\frac{\sqrt{5}}{3}$

7)  $\sin \theta$ , if  $\csc \theta = 1.42716321$

8)  $\tan \theta$ , if  $\cot \theta = 9.80425133$

9) Can a given angle  $\theta$  satisfy both  $\sin \theta > 0$  and  $\csc \theta < 0$ ? Explain.

10) Explain what is wrong with the following item that appears on a trigonometry test:

Find  $\sec \theta$ , given that  $\cos \theta = \frac{3}{2}$ .

11) What is wrong with the following statement?  $\tan 90^\circ = \frac{1}{\cot 90^\circ}$

**Find a value of each variable.**

12)  $\tan(3\theta - 4^\circ) = \frac{1}{\cot(5\theta - 8^\circ)}$

13)  $\sec(2\theta + 6^\circ) \cos(5\theta + 3^\circ) = 1$

14)  $\sin(4\theta + 2^\circ) \csc(3\theta + 5^\circ) = 1$

15)  $\cos(6A + 5^\circ) = \frac{1}{\sec(4A + 15^\circ)}$

**Identify the quadrant or quadrants for the angle satisfying the given conditions.**

16)  $\sin \theta > 0$ ,  $\cos \theta < 0$

17)  $\cos \theta > 0$ ,  $\tan \theta > 0$

18)  $\tan \theta > 0$ ,  $\cot \theta > 0$

19)  $\tan \theta < 0$ ,  $\cot \theta < 0$

20)  $\cos \theta < 0$

21)  $\tan \theta > 0$

**Give the signs of the sine, cosine, and tangent functions for each angle. (Write + or - in the blanks.)**

- |                 |   |                  |   |
|-----------------|---|------------------|---|
| 22) $74^\circ$  | $\sin \rightarrow \underline{\hspace{1cm}}$ , $\cos \rightarrow \underline{\hspace{1cm}}$ , $\tan \rightarrow \underline{\hspace{1cm}}$ | 23) $298^\circ$  | $\sin \rightarrow \underline{\hspace{1cm}}$ , $\cos \rightarrow \underline{\hspace{1cm}}$ , $\tan \rightarrow \underline{\hspace{1cm}}$ |
| 24) $129^\circ$ | $\sin \rightarrow \underline{\hspace{1cm}}$ , $\cos \rightarrow \underline{\hspace{1cm}}$ , $\tan \rightarrow \underline{\hspace{1cm}}$ | 25) $183^\circ$  | $\sin \rightarrow \underline{\hspace{1cm}}$ , $\cos \rightarrow \underline{\hspace{1cm}}$ , $\tan \rightarrow \underline{\hspace{1cm}}$ |
| 26) $406^\circ$ | $\sin \rightarrow \underline{\hspace{1cm}}$ , $\cos \rightarrow \underline{\hspace{1cm}}$ , $\tan \rightarrow \underline{\hspace{1cm}}$ | 27) $412^\circ$  | $\sin \rightarrow \underline{\hspace{1cm}}$ , $\cos \rightarrow \underline{\hspace{1cm}}$ , $\tan \rightarrow \underline{\hspace{1cm}}$ |
| 28) $-82^\circ$ | $\sin \rightarrow \underline{\hspace{1cm}}$ , $\cos \rightarrow \underline{\hspace{1cm}}$ , $\tan \rightarrow \underline{\hspace{1cm}}$ | 29) $-121^\circ$ | $\sin \rightarrow \underline{\hspace{1cm}}$ , $\cos \rightarrow \underline{\hspace{1cm}}$ , $\tan \rightarrow \underline{\hspace{1cm}}$ |

**Decide whether each statement is possible or impossible for an angle  $\theta$ .**

- |                           |                            |                          |
|---------------------------|----------------------------|--------------------------|
| 30) $\sin \theta = 2$     | 31) $\cos \theta = -1.001$ | 32) $\tan \theta = 0.92$ |
| 33) $\cot \theta = -12.1$ | 34) $\sec \theta = 1$      | 35) $\tan \theta = 1$    |

- 36)  $\sin \theta = \frac{1}{2}$  and  $\csc \theta = 2$

- 37)  $\tan \theta = 2$  and  $\cot \theta = -2$

**Use identities to find each function value.**

- |  |   |
|--|---|
| 38) $\tan \theta$ , if $\sec \theta = 3$ , with $\theta$ in quadrant IV            | 39) $\sin \theta$ , if $\cos \theta = -\frac{1}{4}$ , with $\theta$ in quadrant II        |
| 40) $\csc \theta$ , if $\cot \theta = -\frac{1}{2}$ , with $\theta$ in quadrant IV | 41) $\sec \theta$ , if $\tan \theta = \frac{\sqrt{7}}{3}$ , with $\theta$ in quadrant III |
| 42) $\cos \theta$ , if $\csc \theta = -4$ , with $\theta$ in quadrant III          | 43) $\sin \theta$ , if $\sec \theta = 2$ , with $\theta$ in quadrant IV                   |

**Find the values of the six trigonometric functions for each angle.**

- 44) with  $\theta$  in quadrant III      45) with  $\theta$  in quadrant II      46) with  $\theta$  in quadrant III

$$\sin \theta = \underline{\hspace{1cm}} \qquad \sin \theta = \underline{\hspace{1cm}} \qquad \sin \theta = \underline{\hspace{1cm}}$$

$$\cos \theta = -\frac{3}{5} \qquad \cos \theta = \underline{\hspace{1cm}} \qquad \cos \theta = \underline{\hspace{1cm}}$$

$$\tan \theta = \underline{\hspace{1cm}} \qquad \tan \theta = -\frac{15}{8} \qquad \tan \theta = \sqrt{3}$$

$$\csc \theta = \underline{\hspace{1cm}} \qquad \csc \theta = \underline{\hspace{1cm}} \qquad \csc \theta = \underline{\hspace{1cm}}$$

$$\sec \theta = \underline{\hspace{1cm}} \qquad \sec \theta = \underline{\hspace{1cm}} \qquad \sec \theta = \underline{\hspace{1cm}}$$

$$\cot \theta = \underline{\hspace{1cm}} \qquad \cot \theta = \underline{\hspace{1cm}} \qquad \cot \theta = \underline{\hspace{1cm}}$$