Unit 1.3 Notes Using the Definitions of the Trigonometric Functions

## Reciprocal Identities

| Reciprocal Identities |  |  |
| :--- | :--- | :--- |
| $\sin \theta=\frac{1}{\csc \theta}$ | $\cos \theta=\frac{1}{\sec \theta}$ | $\tan \theta=\frac{1}{\cot \theta}$ |
| $\csc \theta=\frac{1}{\sin \theta}$ | $\sec \theta=\frac{1}{\cos \theta}$ | $\cot \theta=\frac{1}{\tan \theta}$ |

## Quotient Identities



Pythagorean Identities

| Pythagorean Identities |  |  |
| :---: | :---: | :---: |
| $\sin ^{2} \theta+\cos ^{2} \theta=1$ |  |  |
| $1+\tan ^{2} \theta=\sec ^{2} \theta$ | $1+\cot ^{2} \theta=\csc ^{2} \theta$ |  |

## Range of Trigonometric Functions

$-1 \leq \sin \theta \leq 1$
$\sec \theta \leq-1$ or $\sec \theta \geq 1$
$\tan \theta$ and $\cot \theta$ can equal any number

$$
-1 \leq \cos \theta \leq 1
$$

$\csc \theta \leq-1$ or $\csc \theta \geq 1$

