

**PRACTICE Quiz 4.1 - 4.2 Fundamental Identities****Verify each identity. Must show all work! Give reason for each step for credit.**

1) 
$$\frac{1}{\csc^2 x \cos x} = \frac{\sin x}{\cot x}$$

2) 
$$\sec^2 x \sin^2 x = \frac{1}{\cot^2 x}$$

$$3) \frac{1 - \sec^2 x}{\sin^2 x} = -\sec^2 x$$

$$4) \frac{\sec^2 x - \tan^2 x}{\cot x} = \sec x \sin x$$

## PRACTICE Quiz 4.1 - 4.2 Fundamental Identities

Verify each identity. Must show all work! Give reason for each step for credit.

$$1) \frac{1}{\csc^2 x \cos x} = \frac{\sin x}{\cot x}$$

$$\frac{1}{\csc^2 x \cos x} \quad \text{Use } \csc x = \frac{1}{\sin x}$$

$$\frac{\sin^2 x}{\cos x} \quad \text{Use } \cot x = \frac{\cos x}{\sin x}$$

$$\frac{\sin x}{\cot x} \quad \blacksquare$$

$$2) \sec^2 x \sin^2 x = \frac{1}{\cot^2 x}$$

$$\sec^2 x \sin^2 x \quad \text{Use } \sec x = \frac{1}{\cos x}$$

$$\frac{\sin^2 x}{\cos^2 x} \quad \text{Use } \cot x = \frac{\cos x}{\sin x}$$

$$\frac{1}{\cot^2 x} \quad \blacksquare$$

$$3) \frac{1 - \sec^2 x}{\sin^2 x} = -\sec^2 x$$

$$\frac{1 - \sec^2 x}{\sin^2 x} \quad \text{Use } \tan^2 x + 1 = \sec^2 x$$

$$-\frac{\tan^2 x}{\sin^2 x} \quad \text{Decompose into sine and cosine}$$

$$-\frac{\left(\frac{\sin x}{\cos x}\right)^2}{\sin^2 x} \quad \text{Simplify}$$

$$-\frac{1}{\cos^2 x} \quad \text{Use } \sec x = \frac{1}{\cos x}$$

$$-\sec^2 x \quad \blacksquare$$

$$4) \frac{\sec^2 x - \tan^2 x}{\cot x} = \sec x \sin x$$

$$\frac{\sec^2 x - \tan^2 x}{\cot x} \quad \text{Use } \tan^2 x + 1 = \sec^2 x$$

$$\frac{1}{\cot x} \quad \text{Use } \cot x = \frac{\cos x}{\sin x}$$

$$\frac{\sin x}{\cos x} \quad \text{Use } \sec x = \frac{1}{\cos x}$$

$$\sec x \sin x \quad \blacksquare$$