

Solve the inequality

$$\begin{array}{r} 3 - 2|a - 3| > -5 \\ -3 \qquad \qquad -3 \end{array}$$

To solve first you need to subtract 3 from both sides

For the next step most people's first instinct is to distribute the -2 into the absolute, but although absolute value is grouping symbols, you can never distribute into the absolute value bars.

So, the only other thing you can do is divide by -2 to both sides,

$$\frac{-2|a - 3|}{-2} > \frac{-8}{-2}$$

This is where the one rule for inequalities is used:

"If you every multiply or divide by a negative number, then flip the inequality sign"

Flipped



$$|a - 3| < 4$$

Once the absolute value is isolated on one side always check for "no solution" and "all real solutions". The absolute value is not < or > a "negative number" so continue.

The absolute value is 4 units away from zero at "4" and "-4"

So write your two inequalities:

Remember to flip the inequality with the negative.

Flipped



Remove the absolute value bars:

$$\begin{array}{r} a - 3 < 4 \\ +3 \quad +3 \end{array}$$

and

$$\begin{array}{r} a - 3 > -4 \\ +3 \quad +3 \end{array}$$

Then finish solving by adding 3 on both sides

Answer!

$$a < 7$$

and

$$a > -1$$

Graph the inequality

On a number line graph the answers:

The numbers used are 7 and -1 from the answers.

If the answer has \leq or \geq then use solid circles: ●

If the answer has $<$ or $>$ then use open circles: ○

So, use open circle to match your answer, put open circle on the 7 and -1

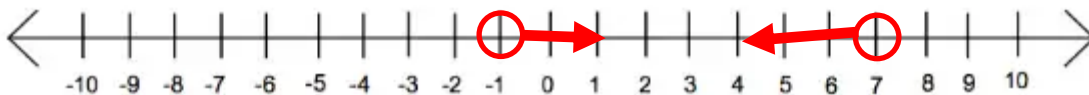


Next, put the arrows on the graph:

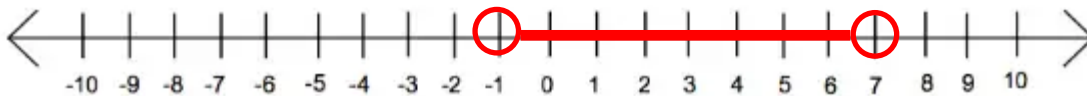
Make sure the variable is on the left, and treat the inequality sign as the arrow direction:

$a < 7$ and $a > -1$

Go left and go right



Since the arrows are going towards each other the connect the lines together



Graph done!

Write the inequality as an interval notation

The numbers used are 7 and -1 and every number in between.

If the answer has \leq or \geq then use brackets: [and]

If the answer has $<$ or $>$ then use parentheses: (and)

So, use parentheses to match your answer, put parentheses around the 7 and -1 and put the 7 and -1 in order as you see them on the number line.

Like so: $(7, -1)$

Done!